Scaling behavior of metal–insulator transitions in a Si/SiGe two dimensional hole gas

C. Possanzini\textsuperscript{a, *}, L. Ponomarenko\textsuperscript{b}, D. de Lang\textsuperscript{b}, A. de Visser\textsuperscript{b}, S.M. Olsthoorn\textsuperscript{a}, R. Fletcher\textsuperscript{c}, Y. Feng\textsuperscript{d}, P.T. Coleridge\textsuperscript{d}, R.L. Williams\textsuperscript{d}, J.C. Maan\textsuperscript{a}

\textsuperscript{a}Research Institute for Materials, High Field Magnet Laboratory, University of Nijmegen, Toernooiveld 1, 6525 ED Nijmegen, Netherlands
\textsuperscript{b}Van der Waals–Zeeman Institute, University of Amsterdam, Valckenierstraat 65, 1018 XE Amsterdam, Netherlands
\textsuperscript{c}Physics Department, Queen’s University, Kingston, Ont., Canada, K7L 3N6
\textsuperscript{d}Institute for Microstructural Sciences, National Research Council, Montreal Road, Ottawa, Ont., Canada K1A 0R6

Abstract

We report the temperature dependence of magnetotransport measurements in a Si/SiGe two-dimensional hole gas (2DHG) and we analyze the curves in terms of scaling. A reentrant insulating transition is observed at filling factor $\nu = 1.5$, followed by a second high field insulating phase at $\nu < 1$. A scaling behavior in temperature of the width of the longitudinal conductivity, its second derivative and the slope of the Hall conductivity has been observed, for both the transitions to the insulating state.

© 2002 Elsevier Science B.V. All rights reserved.

PACS: 71.30.+h, 73.43.Nq

Keywords: Metal–insulator transition; Scaling; SiGe

In a magnetic field, the conductance of a two-dimensional electron system shows vanishing conductivity and quantized Hall plateau, when an integer number of Landau levels are filled. In samples characterized by a short-range scattering potential, like In$_{0.53}$Ga$_{0.47}$As/InP, the transitions between two adjacent plateaus (PP transitions) and between the lowest Landau level and the insulating state in the extreme quantum limit (PI transition) can be all described as quantum critical phenomena \cite{1,2}. In particular, in In$_{0.53}$Ga$_{0.47}$As/InP, the slope of the Hall conductivity and the width of the longitudinal conductivity have been shown to have all the same temperature dependence $\propto T^{-\kappa}$, while the value of the second derivative of the longitudinal conductivity shows a power law dependence on $T$ with a critical exponent of $2\kappa$ [1–3]. For this sample, it was found that the critical exponent is $\kappa = 0.42 \pm 0.04$ and is independent on the Landau level index. Despite the theoretical predictions of the universality of the scaling behavior, such a behavior has been observed only in a few experiments.

In this paper, we report magnetotransport measurements of a low mobility strained p-type Si$_{0.88}$Ge$_{0.12}$/Si heterostructure \cite{4}, which has the same short-range scattering potential as In$_{0.53}$Ga$_{0.47}$As/InP, but a completely different energy level structure. This sample shows not only a Hall-insulator transition in the

\textsuperscript{*} Corresponding author. Fax: +31-24-3652440.
E-mail address: cecilia@sci.kun.nl (C. Possanzini).

1 The present sample is from the growth CVD191 in this paper.
over a wide temperature range for both the longitudinal magnetoresistivity and the longitudinal conductivity. In this paper, we analyze the conductivity measurements and obtained by overlapping the resistance curves. In our measurements, the analysis of the conductivity, through the inversion of the transport matrix, Fig. 1b shows $\sigma_{xx}$ calculated for $p = 2.42 \times 10^{15} \text{ m}^{-2}$ between filling factor 2 and 1: $\sigma_{xx}$ vanishes in both the insulating and in the Hall states and reaches its maximum value at the critical field $B_c$ and $B'_c$. The analysis of the conductivity, which is always finite in the metal–insulator transition, proves to be more accurate than the analysis of the resistance, which diverges in the insulating state. This might explain the different values of the exponents reported in earlier scaling analysis [10,11] and obtained by overlapping the resistance curves. In this paper, we analyze the conductivity measurements over a wide temperature range for both the longitudinal and the Hall conductivity in terms of scaling and we obtain the same critical exponent for the two Hall insulating transitions.

In our measurements, different cooling procedures allow experiments at different carrier density ($p = 1.76 \times 10^{15}$ and $2.42 \times 10^{15} \text{ m}^{-2}$) with the same sample. Fig. 1a shows the magnetoresistance curves for $p = 1.76 \times 10^{15} \text{ m}^{-2}$ in magnetic field up to 12 T and in the temperature range $300 \text{ mK} - 1.2 \text{ K}$.

Fig. 1. (a) Longitudinal magnetoresistivity at different temperatures ($0.3 \text{ K} < T < 1.2 \text{ K}$) for a carrier density $p = 1.76 \times 10^{15} \text{ m}^{-2}$. The inset shows $\sigma_{xy}$ as a function of $\sigma_{xx}$ and demonstrates how the conductivity enters and leaves the insulating state at $v = 1.5$ for different temperatures. (b) The longitudinal conductivity $\sigma_{xx}$ for the insulator transition at filling $v = 1.5$ in the temperature range $70–850 \text{ mK}$ ($p = 2.42 \times 10^{15} \text{ m}^{-2}$).
The value of the critical exponent $\kappa$ in the IP transition is $\kappa = 0.45 \pm 0.05$ for both the densities. The analysis of the slope of the Hall conductivity $(\hat{\sigma}_{xy}/\hat{B})_{B=B_c}$ for $n = 2.42 \times 10^{15}$ m$^{-2}$ (Fig. 2) shows that $(\hat{\sigma}_{xy}/\hat{B})_{B=B_c} \propto T^{-\kappa}$, with $\kappa = 0.45 \pm 0.05$.

According to the scaling theory, if the width of the conductivity $\Delta B$ exhibits a scaling behavior in temperature with an exponent $\kappa$, the second derivative calculated at the critical field should diverge approaching $T = 0$ with the power law $T^{-2\kappa}$. In our measurements, the calculation of the second derivative of the longitudinal conductivity $(\hat{\sigma}_{xx}/\hat{B}^2)_{B=B_c} \propto T^{-2\kappa}$ for both the PI and IP transitions confirms the value of the critical exponent already found for $\Delta B$: $\kappa = 0.45 \pm 0.05$. Fig. 2 summarizes all the results for the exponents of different transitions and densities, obtained by the analysis of experimental curves at different temperatures. It can be seen that the transition to the insulating state and the reentrant insulating phase transition all exhibit the same scaling behavior, with the same critical exponent: $\kappa = 0.45 \pm 0.05$. The critical exponents of the $\sigma_{xx}$ width, the slope of $\sigma_{xy}$ and the second derivative of $\sigma_{xx}$ are the same and, within the experimental error, in agreement with the critical exponents previously observed in InGaAs/InP heterostructures [1–3].

In summary, through an accurate scaling analysis over a wide temperature region, we observed scaling properties for both the reentrant Hall insulator transition at $\nu = 1.5$ and the high field insulating phase transition, at two different densities. Our analysis is based not only on the value of $\sigma_{xx}$ width but also on the first and second derivatives of the conductivity. Since the two transitions show the same scaling behavior, with the same critical exponent, they belong to the same universality class.

We would like to thank Prof. A.M.M. Pruisken and Dr. W. Apel for useful discussions. This work is part of a research program of the Stichting voor Fundamenteel Onderzoek der Materie (FOM) financially supported by NWO (The Netherlands).

References


